

# Optimal Harvesting

**Natural resources for human use:**

**Nonrenewable: fossil fuel, minerals**

**Renewable (Forest, crops, fisheries)**

**over exploitation → exhaustion/ extinction**

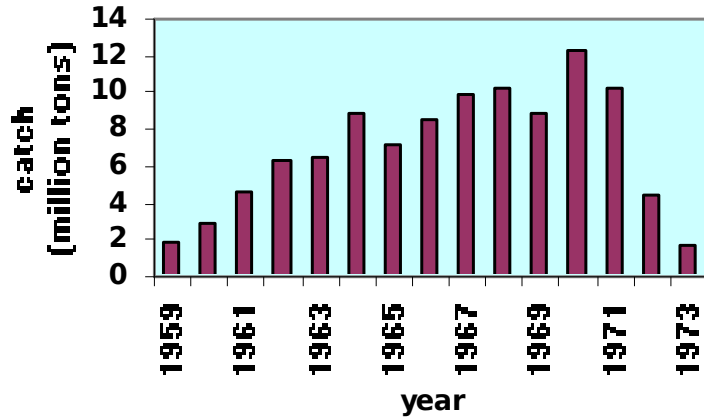
**Whales, anchovies, sugar cane**

## Cases of over-exploitation

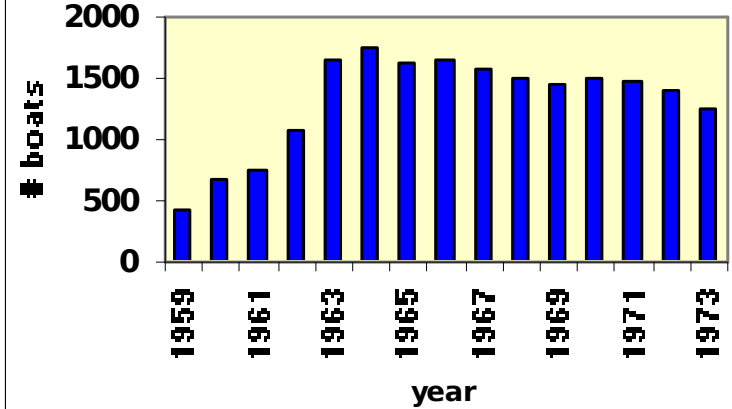
Species	Peak catch	1981 catch
Blue whale(1931)	29,000 (#)	Nil
Fin whales(1938)	27,000 (#)	Nil
Hokkaido herring(1913)	850,000 tons	Nil
California sardine (1936)	640,000 tons	Nil
North sea herring (1962)	1500,000 tons	Negligible

# Peruvian Anchovy Fishery

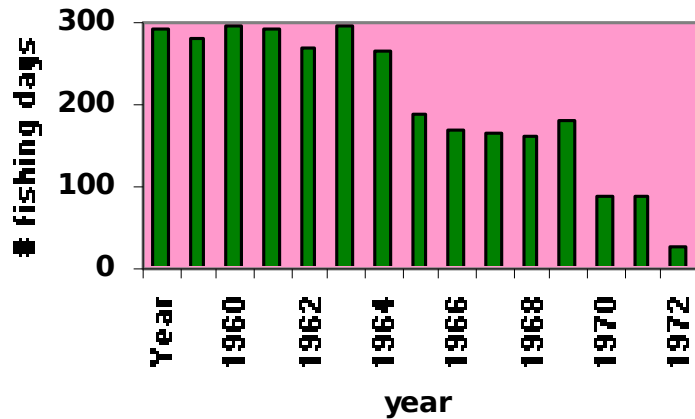
Year wise Total catch



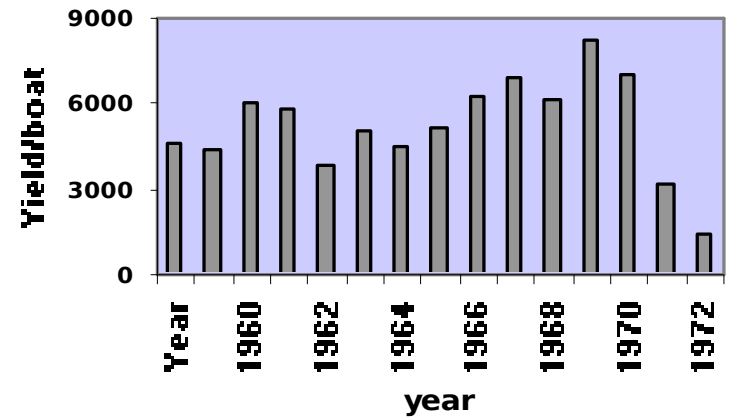
Year wise # boats



Yearwise fishing days



Yearwise catch / boat



**Tuskers poached for ivory- very few left in south India.**

**NTFP collection by tribal groups-  
decline in genetic quality of Amla fruit**

**Sugarcane farming  
soil salinity, over supply**

**Prudent use essential- but how?**

**Tragedy of commons**

**Search for optimal strategy**

**MSY**

# Controversy on export of

Indian bull frog: *Rana tigrina*



Will It disappear?

# Frog-leg Export

Export to : USA, EEC, Japan

Export from : India, Bangladesh, Indonesia etc.

Export from India

Year	volume(tons)
1963	514
1970	2545
1981	4368
1983	3678

## **Pro-export lobby: Traders, MPEDA** **(marine products export development authority)**

Arguments in favor:

- Earning foreign exchange
- Employment in frog catching

Anti export lobby: SPCA, conservationist

Arguments against:

- Threat of frog extinction
- Possible explosion of rice pest population

Policy decision: EXPORT BANNED

Quantitative basis: none to our knowledge

Approach adopted in Gore & Prayag (1993)

Step 1: Estimate density – capture recapture method

Step 2: use population dynamics model with harvesting  
(nonlinear version ) to arrive at optimal strategy  
Biometrics (1975) Doubleday, (1980) Reed



# Density estimation capture – recapture model

- Standard model:

Capture occasion	Before sampling		After sampling	
	Marked	unmarked	Fresh captures	recaptures
First	0	N	R	0
Second	R	N-R	$u_1$	$m_1 = n_1 - u_1$
Third	$(1-k)(R+u_1)$	$(1-k)(N-R-u_1)$	$u_2$	$m_2 = n_2 - u_2$

- $k$  – fraction of frogs removed (harvested)

# Density estimation modified capture – recapture model

- Modified model: introduction of ‘**escapement**’-**e** and compensatory arrivals

Capture occasion	Before sampling		After sampling	
	Marked	unmarked	Fresh captures	recaptures
<b>First</b>	<b>0</b>	<b>N</b>	<b>R</b>	<b>0</b>
<b>Second</b>	<b><math>R(1-e) = R^*</math></b>	<b><math>N-R^*</math></b>	<b><math>u_1</math></b>	<b><math>m_1 = n_1 - u_1</math></b>
<b>Third</b>	<b><math>(1-k)(R^* + u_1 - n_1 e)</math></b>	<b><math>(1-k)(N - R^* - u_1 + n_1 e)</math></b>	<b><math>u_2</math></b>	<b><math>m_2 = n_2 - u_2</math></b>

$p_1 = R^*/N$ ,       $p_2 = (R^* + u_1 - n_1 e) / N$  :  
capture probabilities at 2<sup>nd</sup> and 3<sup>rd</sup> occasion

# Maximum likelihood estimation

- $L(N, e | n_1, n_2, R) = C \cdot p_1^{m_1} (1-p_1)^{u_1} p_2^{m_2} (1-p_2)^{u_2}$

- $N, e$  estimated by search

Estimates in 3 villages of Maharashtra

Village	Est(N)(5ha)	Est(e)	Density/ha
Poinje	539	0.66	107.8
Kolwan	773	0.48	154.6
Kambe	461	0.47	92.2

- Est(e) quite high
- Density 100/ha used for further calculations

# Assessment of sustainable harvest (Doubleday model)

- Leslie matrix approach
  - M- matrix of fecundity & survival
  - $\underline{\theta}$  - diagonal  $(\theta_1, \theta_2, \dots, \theta_{m+1})$   
 $\forall \theta_j$ : fraction from age class j that escapes harvest
  - C – vector of age wise weights
  - V –vector of age structure

- Problem :
  - Maximize  $C'(I - \theta)MV$  (yield)
  - By choosing  $\theta$  such that
  - $\underline{MV} - \underline{V} \geq 0$  increasing population
  - $\forall \theta \underline{MV} - \underline{V} \geq 0$  harvesting stabilizes population
- $\theta$  to be obtained using LPP

# Results

- First attempt:

Age groups: froglets, 1 yr old, 2 yr old, ....6 yr old, above 6 yr

- Harvest policy:  $(I - \theta) = \text{diag}(0.92, 0.02, 0, 0, 1, 1, 1, 1)$

Harvest all 4 yr or older frogs, 92% of froglets

Froglets – useless, yield not worth efforts

If not harvested- population explodes

- This solution not of much practical value

- Modification:
  - Introduce density dependence
    - E- # recruits in froglet class
    - $g(E)$  – proportion surviving
    - $g(E) = \alpha \exp(-\beta E)$
  - A simplifying Constraint
    - all frogs above a threshold age should be harvested
- Good choice 2 years (wt 100gm or above)
- Sustained yield – about 12 Kg/ha
- Matches with field practice of traders

# Effect on insects?

- Argument:
  - Frog – predator of insect
  - Frog harvest may lead to increased insect biomass
- From stomach contents food composition can be estimated

## Food composition of frogs (proportion of body wt)

Frog wt (gm)	crab	insect	larvae
80	0.0134	0.0212	0.0141
125	0.0596	0.0077	0.0027
250	0.0427	0.0067	0.0019
450	0.0442	0.0037	negligible



## Frog population structure

•No harvesting ( 28,28,28,28,8,5,2,1)

•With harvesting  
(our policy) (93,93,0,0,0,0,0,0)

## Food consumption by frogs per day (kg/ha)

	crab	insects	Larvae
No harvest	1.12	0.18	0.08
harvest	0.79	0.25	0.14

• **Harvesting increases insect predation !**

# Findings

- **Optimal strategy: catch frogs of 100 gm or above**
  - **Ensures sustainable yield**
- **Comment: This was the practice of exporters**
  - **Reason: smaller frogs had no demand**
- **Pest control aspect**
  - frog diet- insects and other prey**
  - % share of insects ↓ as weight of frog ↑**
  - large frogs eat crabs**
- **Inference: Removal of large frogs → more small frogs**
  - higher consumption of insects**
  - no danger on pest control front**